## Lecture 11:

## Convolutional Neural Networks




## A closer look at spatial dimensions:



## A closer look at spatial dimensions:



## 7x7 input (spatially) assume $3 \times 3$ filter

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## 7x7 input (spatially) assume 3x3 filter applied with stride 2

## A closer look at spatial dimensions:



## 7x7 input (spatially) assume $3 \times 3$ filter applied with stride 2

## A closer look at spatial dimensions:



## 7x7 input (spatially) assume 3x3 filter applied with stride 2 => $3 x 3$ output!

## A closer look at spatial dimensions:



## 7x7 input (spatially) assume 3x3 filter applied with stride $\mathbf{3 ?}$

## A closer look at spatial dimensions:



# 7x7 input (spatially) assume $3 \times 3$ filter applied with stride $\mathbf{3 ?}$ 

## doesn't fit!

cannot apply $3 x 3$ filter on $7 x 7$ input with stride 3.

|  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  | $F$ |  |  |  |
|  |  |  |  |  |  |  |
|  | F |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |

## Output size: <br> ( N - F ) / stride + 1

e.g. $N=7, F=3$ :
stride $1=>(7-3) / 1+1=5$
stride $2=>(7-3) / 2+1=3$
stride $3=>(7-3) / 3+1=2.33: \$

## In practice: Common to zero pad the border

| 0 | 0 | 0 | 0 | 0 | 0 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |  |

e.g. input $7 \times 7$
$3 \times 3$ filter, applied with stride 1
pad with 1 pixel border => what is the output?

## In practice: Common to zero pad the border

| 0 | 0 | 0 | 0 | 0 | 0 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |  |

e.g. input $7 \times 7$
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## 7x7 output!

## In practice: Common to zero pad the border

| 0 | 0 | 0 | 0 | 0 | 0 |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
| 0 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |

e.g. input $7 x 7$
$3 \times 3$ filter, applied with stride 1
pad with 1 pixel border => what is the output?

## 7x7 output!

in general, common to see CONV layers with stride 1, filters of size FxF, and zero-padding with ( $\mathrm{F}-1$ )/2. (will preserve size spatially)
e.g. $F=3=>$ zero pad with 1

F = $5=>$ zero pad with 2
F = 7 => zero pad with 3

## Remember back to...

E.g. 32x32 input convolved repeatedly with $5 \times 5$ filters shrinks volumes spatially! (32-> 28 -> 24 ...). Shrinking too fast is not good, doesn't work well.


## Examples time:

## Input volume: 32x32x3 $105 \times 5$ filters with stride 1 , pad 2



## Output volume size: ?

## Examples time:

## Input volume: 32x32x3 $105 \times 5$ filters with stride 1, pad 2



Output volume size:
$\left(32+2^{*} 2-5\right) / 1+1=32$ spatially, so
32x32x10

## Examples time:

## Input volume: 32x32x3 $105 \times 5$ filters with stride 1 , pad 2



## Number of parameters in this layer?

## Examples time:

## Input volume: 32x32x3 $105 \times 5$ filters with stride 1 , pad 2



Number of parameters in this layer? each filter has $5 * 5 * 3+1=76$ params ( +1 for bias) => $76 * 10=760$

Summary. To summarize, the Conv Layer:

- Accepts a volume of size $W_{1} \times H_{1} \times D_{1}$
- Requires four hyperparameters:
- Number of filters $K$,
- their spatial extent $F$,
- the stride $S$,
- the amount of zero padding $P$.
- Produces a volume of size $W_{2} \times H_{2} \times D_{2}$ where:
- $W_{2}=\left(W_{1}-F+2 P\right) / S+1$
- $H_{2}=\left(H_{1}-F+2 P\right) / S+1$ (i.e. width and height are computed equally by symmetry)
- $D_{2}=K$
- With parameter sharing, it introduces $F \cdot F \cdot D_{1}$ weights per filter, for a total of $\left(F \cdot F \cdot D_{1}\right) \cdot K$ weights and $K$ biases.
- In the output volume, the $d$-th depth slice (of size $W_{2} \times H_{2}$ ) is the result of performing a valid convolution of the $d$-th filter over the input volume with a stride of $S$, and then offset by $d$-th bias.


## Common settings:

Summary. To summarize, the Conv Layer:

$$
\begin{aligned}
K= & \text { (powers of } 2, \text { e.g. } 32,64,128,512) \\
- & F=3, S=1, P=1 \\
- & F=5, S=1, P=2 \\
- & F=5, S=2, P=? \text { (whatever fits) } \\
- & F=1, S=1, P=0
\end{aligned}
$$

- Accepts a volume of size $W_{1} \times H_{1} \times D_{1}$
- Requires four hyperparameters:
- Number of filters $K$,
- their spatial extent $F$,
- the stride $S$
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- In the output volume, the $d$-th depth slice (of size $W_{2} \times H_{2}$ ) is the result of performing a valid convolution of the $d$-th filter over the input volume with a stride of $S$, and then offset by $d$-th bias.
(btw, $1 \times 1$ convolution layers make perfect sense)




## Pooling layer

- makes the representations smaller and more manageable
- operates over each activation map independently:



## MAX POOLING

## Single depth slice


max pool with $2 \times 2$ filters and stride 2


- Accepts a volume of size $W_{1} \times H_{1} \times D_{1}$
- Requires three hyperparameters:
- their spatial extent $F$,
- the stride $S$,
- Produces a volume of size $W_{2} \times H_{2} \times D_{2}$ where:
- $W_{2}=\left(W_{1}-F\right) / S+1$
- $H_{2}=\left(H_{1}-F\right) / S+1$
- $D_{2}=D_{1}$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers


## Common settings:

- Accepts a volume of size $W_{1} \times H_{1} \times D_{1}$
- Requires three hyperparameters:
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- $D_{2}=D_{1}$
- Introduces zero parameters since it computes a fixed function of the input
- Note that it is not common to use zero-padding for Pooling layers

$$
\begin{aligned}
& F=2, S=2 \\
& F=3, S=2
\end{aligned}
$$

## Why do we need pooling?

- Pool information by increasing receptive field
- Provide some spatial invariance


## Fully Connected Layer (FC layer)

- Contains neurons that connect to the entire input volume, as in ordinary Neural Networks



## [ConvNetJS demo: training on CIFAR-10]

## http://cs.stanford.edu/people/karpathy/convnetis/demo/cifar10.html

## Receptive field

Which pixels in the input image have impact on the value of $\mathbf{v}$ ?


## Receptive field

Which pixels in the input image have impact on the value of $\mathbf{v}$ ?
With POOL Layers?


## Dilated convolution, for even larger receptive fields


(a)

(b)

(c)

Figure 1: Systematic dilation supports exponential expansion of the receptive field without loss of resolution or coverage. (a) $F_{1}$ is produced from $F_{0}$ by a 1-dilated convolution; each element in $F_{1}$ has a receptive field of $3 \times 3$. (b) $F_{2}$ is produced from $F_{1}$ by a 2-dilated convolution; each element in $F_{2}$ has a receptive field of $7 \times 7$. (c) $F_{3}$ is produced from $F_{2}$ by a 4 -dilated convolution; each element in $F_{3}$ has a receptive field of $15 \times 15$. The number of parameters associated with each layer is identical. The receptive field grows exponentially while the number of parameters grows linearly.

## Multi-Scale Context Aggregation by Dilated Convolutions, Fisher Yu, Vladlen Koltun

## Case Study: LeNet-5

[LeCun et al., 1998]


Conv filters were $5 \times 5$, applied at stride 1
Subsampling (Pooling) layers were $2 \times 2$ applied at stride 2
i.e. architecture is [CONV-POOL-CONV-POOL-CONV-FC]

## Case Study: AlexNet

[Krizhevsky et al. 2012]


Input: 227x227x3 images
First layer (CONV1): 96 11x11 filters applied at stride 4
=>
Q: what is the output volume size? Hint: $(227-11) / 4+1=55$

## Case Study: AlexNet

[Krizhevsky et al. 2012]


Input: 227x227x3 images
First layer (CONV1): 96 11x11 filters applied at stride 4
=>
Output volume [55x55x96]
Q: What is the total number of parameters in this layer?

## Case Study: AlexNet

[Krizhevsky et al. 2012]


Input: 227x227x3 images
First layer (CONV1): 96 11x11 filters applied at stride 4
=>
Output volume [55x55x96]
Parameters: $\left(11^{*} 11^{*} 3\right)^{*} 96=35 \mathrm{~K}$

## Case Study: AlexNet

[Krizhevsky et al. 2012]


Input: 227x227x3 images
After CONV1: 55x55x96
Second layer (POOL1): $3 \times 3$ filters applied at stride 2
Q: what is the output volume size? Hint: $(55-3) / 2+1=27$

## Case Study: AlexNet

[Krizhevsky et al. 2012]


Input: 227x227x3 images
After CONV1: 55x55x96
Second layer (POOL1): $3 \times 3$ filters applied at stride 2 Output volume: 27x27x96

Q: what is the number of parameters in this layer?

## Case Study: AlexNet

[Krizhevsky et al. 2012]


Input: 227x227x3 images
After CONV1: 55x55x96
Second layer (POOL1): $3 \times 3$ filters applied at stride 2
Output volume: 27x27x96
Parameters: 0!

## Case Study: AlexNet

[Krizhevsky et al. 2012]


Input: 227x227x3 images
After CONV1: 55x55x96
After POOL1: $27 \times 27 \times 96$

## Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture: [227x227x3] INPUT

[55x55x96] CONV1: $9611 \times 11$ filters at stride 4, pad 0
[27x27x96] MAX POOL1: $3 \times 3$ filters at stride 2
[27x27x96] NORM1: Normalization layer
[27x27x256] CONV2: $2565 \times 5$ filters at stride 1, pad 2
[13x13x256] MAX POOL2: $3 \times 3$ filters at stride 2
[13×13x256] NORM2: Normalization layer
[13×13×384] CONV3: $3843 \times 3$ filters at stride 1, pad 1
[13x13x384] CONV4: $3843 \times 3$ filters at stride 1, pad 1
[13×13x256] CONV5: $2563 \times 3$ filters at stride 1, pad 1
[6x6x256] MAX POOL3: $3 \times 3$ filters at stride 2
[4096] FC6: 4096 neurons
[4096] FC7: 4096 neurons
[1000] FC8: 1000 neurons (class scores)

## Case Study: AlexNet

[Krizhevsky et al. 2012]

Full (simplified) AlexNet architecture: [227x227x3] INPUT

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[13x13x256] MAX POOL2: $3 \times 3$ filters at stride 2
[13×13x256] NORM2: Normalization layer
[13×13×384] CONV3: $3843 \times 3$ filters at stride 1, pad 1
[13×13×384] CONV4: $3843 \times 3$ filters at stride 1, pad 1
[13×13x256] CONV5: $2563 \times 3$ filters at stride 1, pad 1
[6x6x256] MAX POOL3: 3x3 filters at stride 2
[4096] FC6: 4096 neurons
[4096] FC7: 4096 neurons
[1000] FC8: 1000 neurons (class scores)

## Case Study: ZFNet [Zeiere and Fergus, 2013$]$



Input Image


Layer 2



Layer 4

Layer 6 Layer 7

Output

AlexNet but:
CONV1: change from ( $11 \times 11$ stride 4 ) to ( $7 \times 7$ stride 2)
CONV3,4,5: instead of 384, 384, 256 filters use 512, 1024, 512 ImageNet top 5 error: 15.4\% -> 14.8\%

## Case Study: VGGNet

[Simonyan and Zisserman, 2014]
Only $3 x 3$ CONV stride 1, pad 1 and $2 x 2$ MAX POOL stride 2

## best model

## 11.2\% top 5 error in ILSVRC 2013

| ConvNet Configuration |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| A | A-LRN | B | C | D | E |
| 11 weight layers | 11 weight layers | 13 weight layers | $\begin{gathered} \hline 16 \text { weight } \\ \text { layers } \\ \hline \end{gathered}$ | $\begin{gathered} 16 \text { weight } \\ \text { layers } \\ \hline \end{gathered}$ | $\begin{gathered} 19 \text { weight } \\ \text { layers } \\ \hline \end{gathered}$ |
| input ( $224 \times 224$ RGB imag ) |  |  |  |  |  |
| conv3-64 | $\begin{aligned} & \hline \text { conv3-64 } \\ & \text { LRN } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-64 } \\ & \text { conv3-64 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-64 } \\ & \text { conv3-64 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-64 } \\ & \text { conv3-64 } \end{aligned}$ | $\begin{aligned} & \text { conv3-64 } \\ & \text { conv3-64 } \end{aligned}$ |
| maxpool |  |  |  |  |  |
| conv3-128 | conv3-128 | $\begin{aligned} & \text { conv3-128 } \\ & \text { conv3-128 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-128 } \\ & \text { conv3-128 } \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { conv3-128 } \\ & \text { conv3-128 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-128 } \\ & \text { conv3-128 } \\ & \hline \end{aligned}$ |
| maxpool |  |  |  |  |  |
| $\begin{aligned} & \text { conv3-256 } \\ & \text { conv3-256 } \end{aligned}$ | $\begin{aligned} & \text { conv3-256 } \\ & \text { conv3-256 } \end{aligned}$ | $\begin{aligned} & \text { conv3-256 } \\ & \text { conv3-256 } \end{aligned}$ | $\begin{array}{\|l\|} \hline \begin{array}{l} \text { conv3-256 } \\ \text { conv3-256 } \end{array} \\ \hline \text { conv1-256 } \end{array}$ | $\begin{aligned} & \text { conv3-256 } \\ & \text { conv3-256 } \\ & \text { conv3-256 } \end{aligned}$ | $\begin{aligned} & \text { conv3-256 } \\ & \text { conv3-256 } \\ & \text { conv3-256 } \\ & \text { conv3-256 } \\ & \hline \end{aligned}$ |
| maxpool |  |  |  |  |  |
| $\begin{aligned} & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv1-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | conv3-512 <br> conv3-512 <br> conv3-512 <br> conv3-512 |
| maxpool |  |  |  |  |  |
| $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv1-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ |
| maxpool |  |  |  |  |  |
| FC-4096 |  |  |  |  |  |
| FC-4096 |  |  |  |  |  |
| FC-1000 |  |  |  |  |  |
| soft-max |  |  |  |  |  |

->
$7.3 \%$ top 5 error
Table 2: Number of parameters (in millions).

| Network | A,A-LRN | B | C | D | E |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Number of parameters | 133 | 133 | 134 | 138 | 144 |

INPUT: [224×224x3] memory: $224 * 224 * 3=150 \mathrm{~K}$ params: 0
(not counting biases)
CONV3-64: [224×224x64] memory: 224*224*64=3.2M params: $\left(3^{*} 3 * 3\right)^{*} 64=1,728$
CONV3-64: [224x224x64] memory: 224*224*64=3.2M params: (3*3*64)*64 $=36,864$
POOL2: [112x112x64] memory: 112*112*64=800K params: 0
CONV3-128: [112×112x128] memory: $112^{*} 112^{*} 128=1.6 \mathrm{M}$ params: $\left(3^{*} 3^{*} 64\right)^{*} 128=73,728$
CONV3-128: $[112 \times 112 \times 128]$ memory: $112^{*} 112^{*} 128=1.6 \mathrm{M}$ params: $\left(3^{*} 3^{*} 128\right)^{*} 128=147,456$
POOL2: [56x56x128] memory: 56*56*128=400K params: 0
CONV3-256: [56x56x256] memory: $56 * 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 128\right)^{*} 256=294,912$
CONV3-256: [56x56x256] memory: $56 * 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 256=589,824$
CONV3-256: [56x56x256] memory: $56^{*} 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 256=589,824$
POOL2: [28x28×256] memory: 28*28*256=200K params: 0
CONV3-512: [28x28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 512=1,179,648$
CONV3-512: [28x28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
CONV3-512: [28x28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$ POOL2: [14x14×512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: 0
CONV3-512: [14x14x512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $(3 * 3 * 512)^{*} 512=2,359,296$ CONV3-512: [14x14x512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$ CONV3-512: [14x14x512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$ POOL2: [7x7x512] memory: $7^{*} 7^{*} 512=25 \mathrm{~K}$ params: 0
FC: [1x1x4096] memory: 4096 params: $7^{*} 7^{*} 512^{*} 4096=102,760,448$
FC: [1x1x4096] memory: 4096 params: $4096 * 4096=16,777,216$
FC: [1x1x1000] memory: 1000 params: $4096 * 1000=4,096,000$

| ConvNet Configuration |  |  |  |
| :---: | :---: | :---: | :---: |
| B | C | D |  |
| 13 weight layers | 16 weight layers | 16 weight layers | 19 |
| put ( $224 \times 224$ RGB image |  |  |  |
| $\begin{aligned} & \hline \text { conv3-64 } \\ & \text { conv3-64 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-64 } \\ & \text { conv3-64 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-64 } \\ & \text { conv3-64 } \end{aligned}$ | cc cc |
| maxpool |  |  |  |
| $\begin{aligned} & \hline \text { conv3-128 } \\ & \text { conv3-128 } \end{aligned}$ | $\begin{aligned} & \text { conv3-128 } \\ & \text { conv3-128 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-128 } \\ & \text { conv3-128 } \end{aligned}$ | co co |
| maxpool |  |  |  |
| $\begin{aligned} & \hline \text { conv3-256 } \\ & \text { conv3-256 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-256 } \\ & \text { conv3-256 } \\ & \text { conv1-256 } \end{aligned}$ | $\begin{aligned} & \text { conv3-256 } \\ & \text { conv3-256 } \\ & \text { conv3-256 } \end{aligned}$ | co co co |
| maxpool |  |  |  |
| $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv1-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | co co co |
| maxpool |  |  |  |
| $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv1-512 } \end{aligned}$ | $\begin{aligned} & \hline \text { conv3-512 } \\ & \text { conv3-512 } \\ & \text { conv3-512 } \end{aligned}$ | co co co |
| maxpool |  |  |  |
| FC-4096 |  |  |  |
| FC-4096 |  |  |  |
| FC-1000 |  |  |  |
| soft-max |  |  |  |

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CONV3-64: [224x224x64] memory: $224^{*} 224^{*} 64=3.2 \mathrm{M}$ params: $\left(3^{*} 3^{*} 64\right)^{*} 64=36,864$
POOL2: [112x112x64] memory: 112*112*64=800K params: 0
CONV3-128: [112×112×128] memory: $112^{*} 112^{*} 128=1.6 \mathrm{M}$ params: $\left(3^{*} 3^{*} 64\right)^{*} 128=73,728$
CONV3-128: $[112 \times 112 \times 128]$ memory: $112^{*} 112^{*} 128=1.6 \mathrm{M}$ params: $\left(3^{*} 3^{*} 128\right)^{*} 128=147,456$
POOL2: [56x56x128] memory: 56*56*128=400K params: 0
CONV3-256: [56x56x256] memory: $56 * 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 128\right)^{*} 256=294,912$
CONV3-256: [56x56x256] memory: $56 * 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 256=589,824$
CONV3-256: [56x56x256] memory: $56^{*} 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 256=589,824$
POOL2: [28x28×256] memory: 28*28*256=200K params: 0
CONV3-512: [28x28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 512=1,179,648$
CONV3-512: [28×28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
CONV3-512: [28x28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
POOL2: [14x14×512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: 0
CONV3-512: [14x14x512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $(3 * 3 * 512)^{*} 512=2,359,296$
CONV3-512: [14x14x512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
CONV3-512: [14x14x512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
POOL2: [7x7x512] memory: $7^{*} 7^{*} 512=25 \mathrm{~K}$ params: 0
FC: [1x1x4096] memory: 4096 params: $7^{*} 7^{*} 512^{*} 4096=102,760,448$
FC: [1x1x4096] memory: 4096 params: $4096 * 4096=16,777,216$
FC: [1x1x1000] memory: 1000 params: $4096 * 1000=4,096,000$
TOTAL memory: $24 \mathrm{M} * 4$ bytes $\sim=93 \mathrm{MB}$ / image (only forward! $\sim^{*} 2$ for bwd)
TOTAL params: 138M parameters

CONV3-64: [224x224x64] memory: $224^{*} 224 * 64=3.2 \mathrm{M}$ params: $\left(3^{*} 3^{*} 64\right)^{*} 64=36,864$
POOL2: [112x112x64] memory: 112*112*64=800K params: 0
CONV3-128: [112×112x128] memory: $112^{*} 112^{*} 128=1.6 \mathrm{M}$ params: $\left(3^{*} 3^{*} 64\right)^{*} 128=73,728$
CONV3-128: [112x112x128] memory: $112^{* 112 * 128=1.6 M ~ p a r a m s: ~}\left(3^{*} 3^{*} 128\right)^{*} 128=147,456$
POOL2: [56x56x128] memory: 56*56*128=400K params: 0
CONV3-256: [56x56x256] memory: $56 * 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 128\right)^{*} 256=294,912$
CONV3-256: [56x56x256] memory: $56 * 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 256=589,824$
CONV3-256: [56x56x256] memory: $56 * 56^{*} 256=800 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 256=589,824$
POOL2: [28x28×256] memory: $28^{*} 28^{*} 256=200 \mathrm{~K}$ params: 0
CONV3-512: [28x28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 256\right)^{*} 512=1,179,648$
CONV3-512: [28×28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
CONV3-512: [28x28x512] memory: $28^{*} 28^{*} 512=400 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
POOL2: [14x14×512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: 0
CONV3-512: [14×14×512] memory: $14 * 14 * 512=100 \mathrm{~K}$ params: $(3 * 3 * 512)^{*} 512=2,359,296$
CONV3-512: [14×14×512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
CONV3-512: [14×14×512] memory: $14^{*} 14^{*} 512=100 \mathrm{~K}$ params: $\left(3^{*} 3^{*} 512\right)^{*} 512=2,359,296$
POOL2: [7x7x512] memory: $7^{*} 7 * 512=25 \mathrm{~K}$ params: 0
Most memory is in early CONV

FC: $[1 \times 1 \times 4096]$ memory: 4096 params: $7^{*} 7^{*} 512^{*} 4096=\mathbf{1 0 2 , 7 6 0 , 4 4 8}$
FC: [1x1x4096] memory: 4096 params: $4096 * 4096=16,777,216$
FC: [1x1x1000] memory: 1000 params: $4096 * 1000=4,096,000$
TOTAL memory: $24 \mathrm{M} * 4$ bytes $\sim=93 \mathrm{MB}$ / image (only forward! $\sim * 2$ for bwd)
TOTAL params: 138M parameters

## Case Study: GoogLeNet



Inception module

ILSVRC 2014 winner (6.7\% top 5 error)

## Case Study: GoogLeNet

| type | patch size/ stride | $\begin{gathered} \hline \text { output } \\ \text { size } \\ \hline \end{gathered}$ | depth | $\# 1 \times 1$ | $\# 3 \times 3$ <br> reduce | $\# 3 \times 3$ | $\# 5 \times 5$ <br> reduce | $\# 5 \times 5$ | pool <br> proj | params | ops |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| convolution | $7 \times 7 / 2$ | $112 \times 112 \times 64$ | 1 |  |  |  |  |  |  | 2.7 K | 34 M |
| max pool | $3 \times 3 / 2$ | $56 \times 56 \times 64$ | 0 |  |  |  |  |  |  |  |  |
| convolution | $3 \times 3 / 1$ | $56 \times 56 \times 192$ | 2 |  | 64 | 192 |  |  |  | 112 K | 360M |
| max pool | $3 \times 3 / 2$ | $28 \times 28 \times 192$ | 0 |  |  |  |  |  |  |  |  |
| inception (3a) |  | $28 \times 28 \times 256$ | 2 | 64 | 96 | 128 | 16 | 32 | 32 | 159 K | 128 M |
| inception (3b) |  | $28 \times 28 \times 480$ | 2 | 128 | 128 | 192 | 32 | 96 | 64 | 380K | 304M |
| max pool | $3 \times 3 / 2$ | $14 \times 14 \times 480$ | 0 |  |  |  |  |  |  |  |  |
| inception (4a) |  | $14 \times 14 \times 512$ | 2 | 192 | 96 | 208 | 16 | 48 | 64 | 364 K | 73 M |
| inception (4b) |  | $14 \times 14 \times 512$ | 2 | 160 | 112 | 224 | 24 | 64 | 64 | 437 K | 88 M |
| inception (4c) |  | $14 \times 14 \times 512$ | 2 | 128 | 128 | 256 | 24 | 64 | 64 | 463 K | 100 M |
| inception (4d) |  | $14 \times 14 \times 528$ | 2 | 112 | 144 | 288 | 32 | 64 | 64 | 580 K | 119M |
| inception (4e) |  | $14 \times 14 \times 832$ | 2 | 256 | 160 | 320 | 32 | 128 | 128 | 840K | 170M |
| max pool | $3 \times 3 / 2$ | $7 \times 7 \times 832$ | 0 |  |  |  |  |  |  |  |  |
| inception (5a) |  | $7 \times 7 \times 832$ | 2 | 256 | 160 | 320 | 32 | 128 | 128 | 1072K | 54 M |
| inception (5b) |  | $7 \times 7 \times 1024$ | 2 | 384 | 192 | 384 | 48 | 128 | 128 | 1388 K | 71 M |
| avg pool | $7 \times 7 / 1$ | $1 \times 1 \times 1024$ | 0 |  |  |  |  |  |  |  |  |
| dropout (40\%) |  | $1 \times 1 \times 1024$ | 0 |  |  |  |  |  |  |  |  |
| linear |  | $1 \times 1 \times 1000$ | 1 |  |  |  |  |  |  | 1000 K | 1M |
| softmax |  | $1 \times 1 \times 1000$ | 0 |  |  |  |  |  |  |  |  |

## Fun features:

- Only 5 million params! (Removes FC layers completely)

Compared to AlexNet:

- 12X less params
- $2 x$ more compute
- $6.67 \%$ (vs. 16.4\%)


## Case Study: ResNet <br> ILSVRC 2015 winner ( $3.6 \%$ top 5 error)

```
Research
```


## MSRA @ ILSVRC \& COCO 2015 Competitions

```
- 1st places in all five main tracks
- ImageNet Classification: "Ultra-deep" (quote Yann) 152-layer nets
- ImageNet Detection: 16\% better than 2nd
- ImageNet Localization: 27\% better than 2nd
- COCO Detection: 11\% better than 2nd
- COCO Segmentation: 12\% better than 2nd
```


## Deep Residual Learning for Image Recognition

Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun

(slide from Kaiming He's recent presentation)

## CIFAR-10 experiments

CIFAR-10 plain nets


CIFAR-10 ResNets


## Case Study: ResNet [He et al, 2015$]$

ILSVRC 2015 winner ( $3.6 \%$ top 5 error)


Research<br>2-3 weeks of training on 8 GPU machine<br>at runtime: faster than a VGGNet! (even though it has 8x more layers)

(slide from Kaiming He's presentation)

## Case Study: ResNet

[He et al., 2015]

34-layer plain


34-layer residual


## Case Study: ResNet [He et al., 2015]



## Case Study: ResNet [He et al., 2015]

- Batch Normalization after every CONV layer
- Xavier/2 initialization from He et al.
- SGD + Momentum (0.9)
- Learning rate: 0.1, divided by 10 when validation error plateaus
- Mini-batch size 256
- Weight decay of 1 e-5
- No dropout used


## Case Study: ResNet [He etal, 2015



## Case Study: ResNet IHe etal, 2015]


(this trick is also used in GoogLeNet)

|  | Sasestury Resmet [He et al., 2015] |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | layer name | output size | 18-layer | 34-layer | 50-layer | 101-layer | 152-layer |
| \% | conv1 | $112 \times 112$ | $7 \times 7,64$, stride 2 |  |  |  |  |
|  |  |  | $3 \times 3$ max pool, stride 2 |  |  |  |  |
|  | conv2_x | $56 \times 56$ | $\left[\begin{array}{l}3 \times 3,64 \\ 3 \times 3,64\end{array}\right] \times 2$ | $\left[\begin{array}{l}3 \times 3,64 \\ 3 \times 3,64\end{array}\right] \times 3$ | $\left[\begin{array}{c}1 \times 1,64 \\ 3 \times 3,64 \\ 1 \times 1,256\end{array}\right] \times 3$ | $\left[\begin{array}{c}1 \times 1,64 \\ 3 \times 3,64 \\ 1 \times 1,256\end{array}\right] \times 3$ | $\left[\begin{array}{c}1 \times 1,64 \\ 3 \times 3,64 \\ 1 \times 1,256\end{array}\right] \times 3$ |
|  | conv3_x | $28 \times 28$ | $\left[\begin{array}{l}3 \times 3,128 \\ 3 \times 3,128\end{array}\right] \times 2$ | $\left[\begin{array}{l}3 \times 3,128 \\ 3 \times 3,128\end{array}\right] \times 4$ | $\left[\begin{array}{l}1 \times 1,128 \\ 3 \times 3,128 \\ 1 \times 1,512\end{array}\right] \times 4$ | $\left[\begin{array}{l}1 \times 1,128 \\ 3 \times 3,128 \\ 1 \times 1,512\end{array}\right] \times 4$ | $\left[\begin{array}{l}1 \times 1,128 \\ 3 \times 3,128 \\ 1 \times 1,512\end{array}\right] \times 8$ |
|  | conv4_x | $14 \times 14$ | $\left[\begin{array}{l}3 \times 3,256 \\ 3 \times 3,256\end{array}\right] \times 2$ | $\left[\begin{array}{l}3 \times 3,256 \\ 3 \times 3,256\end{array}\right] \times 6$ | $\left[\begin{array}{c}1 \times 1,256 \\ 3 \times 3,256 \\ 1 \times 1,1024\end{array}\right] \times 6$ | $\left[\begin{array}{c}1 \times 1,256 \\ 3 \times 3,256 \\ 1 \times 1,1024\end{array}\right] \times 23$ | $\left[\begin{array}{c}1 \times 1,256 \\ 3 \times 3,256 \\ 1 \times 1,1024\end{array}\right] \times 36$ |
|  | conv5_x | $7 \times 7$ | $\left[\begin{array}{l}3 \times 3,512 \\ 3 \times 3,512\end{array}\right] \times 2$ | $\left[\begin{array}{l}3 \times 3,512 \\ 3 \times 3,512\end{array}\right] \times 3$ | $\left[\begin{array}{c}1 \times 1,512 \\ 3 \times 3,512 \\ 1 \times 1,2048\end{array}\right] \times 3$ | $\left[\begin{array}{c}1 \times 1,512 \\ 3 \times 3,512 \\ 1 \times 1,2048\end{array}\right] \times 3$ | $\left[\begin{array}{c}1 \times 1,512 \\ 3 \times 3,512 \\ 1 \times 1,2048\end{array}\right] \times 3$ |
|  |  | $1 \times 1$ | average pool, $1000-\mathrm{d} \mathrm{fc}$, softmax |  |  |  |  |
|  | FLOPs |  | $1.8 \times 10^{9}$ | $3.6 \times 10^{9}$ | $3.8 \times 10^{9}$ | $7.6 \times 10^{9}$ | $11.3 \times 10^{9}$ |

## Case Study: ResNet teeala, 2015

Subhransu Maji, Chuang Gan and TAs
Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller

## Summary

- ConvNets stack CONV,POOL,FC layers
- Trend towards smaller filters and deeper architectures
- Trend towards getting rid of POOL/FC layers (just CONV)
- Typical architectures look like [(CONV-RELU)*N-POOL?]*M-(FC-RELU)*K,SOFTMAX where N is usually up to $\sim 5, \mathrm{M}$ is large, $0<=\mathrm{K}<=2$.
- but recent advances such as ResNet/GoogLeNet challenge this paradigm

