# Lecture 3: Loss functions and Optimization

Subhransu Maji, Chuang Gan and TAs Some slides kindly provided by Fei-Fei Li, Jiajun Wu, Erik Learned-Miller Lecture 3 - 1 Sept. 12, 2023

## Homework 1

- Due on 9/28 (Th.) 11:55 pm
- Submit via gradescope
  - We will enroll you on gradescope this week

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# **First Optional Discussion Section**

- This Friday ??am. Led by TA Max Hamilton.
- Topic: Slicing and broadcasting in Python:
  - Example:
    - A is a 5x8 array.
    - B is a 1x8 array.
    - A+B in python will replicate B 5 times to make it the same size as A before adding.

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- This is "broadcasting".
- Try to read NumPy Tutorial sections on Indexing and Broadcasting before you get there. Try some examples.

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#### Recall from last time ... Linear classifier



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## **Loss function/Optimization**





airplane	-3.45	-0.51	3.42
automobile	-8.87	6.04	4.64
bird	0.09	5.31	2.65
cat	2.9	-4.22	5.1
deer	4.48	-4.19	2.64
dog	8.02	3.58	5.55
free	3.78	4.49	-4.34
irog	1.06	-4.37	-1.5
horse	-0.36	-2.09	-4.79
ship	-0.72	-2.93	6.14
truck			

### TODO:

- 1. Define a **loss function** that quantifies our unhappiness with the scores across the training data.
- Come up with a way of efficiently finding the parameters that minimize the loss function. (optimization)

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cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1

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#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

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#### **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$\begin{split} L_i &= \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + 1) \\ &= \max(0, 5.1 - 3.2 + 1) \\ &+ \max(0, -1.7 - 3.2 + 1) \\ &= \max(0, 2.9) + \max(0, -3.9) \\ &= 2.9 + 0 \\ &= 2.9 \end{split}$$

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#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$\begin{split} L_i &= \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + 1) \\ &= \max(0, 1.3 - 4.9 + 1) \\ &+ \max(0, 2.0 - 4.9 + 1) \\ &= \max(0, -2.6) + \max(0, -1.9) \\ &= 0 + 0 \\ &= 0 \end{split}$$

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#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + 1)$$
  
= max(0, 2.2 - (-3.1) + 1)  
+max(0, 2.5 - (-3.1) + 1)  
= max(0, 6.3) + max(0, 6.6)

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#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

 $L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$ 

and the full training loss is the mean over all examples in the training data:

$$L = rac{1}{N} \sum_{i=1}^N L_i$$

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#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

 $L_i = \sum_{j \neq y_i} \max(0, s_j - s_{y_i} + 1)$ Q: what if the sum was instead over all classes? (including j = y\_i)

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#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q2: what if we used a mean instead of a sum here?

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cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	12.9

#### **Multiclass SVM loss:**

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q3: what if we used

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)^2$$

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#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q4: what is the min/ max possible loss?

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cat	3.2	1.3	2.2
car	5.1	4.9	2.5
frog	-1.7	2.0	-3.1
Losses:	2.9	0	12.9

#### Multiclass SVM loss:

Given an example  $(x_i, y_i)$ where  $x_i$  is the image and where  $y_i$  is the (integer) label,

and using the shorthand for the scores vector:  $s_i = f(x_i, W)$ 

the SVM loss has the form:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

Q5: usually at initialization W are small numbers, so all s ~= 0. What is the loss?

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Example numpy code:

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

```
def L_i_vectorized(x, y, W):
    scores = W.dot(x)
    margins = np.maximum(0, scores - scores[y] + 1)
    margins[y] = 0
    loss_i = np.sum(margins)
    return loss_i
```

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#### Coding tip: Keep track of dimensions:



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There is a "bug" with the loss:

 $egin{aligned} f(x,W) &= Wx \ L &= rac{1}{N} \sum_{i=1}^N \sum_{j 
eq y_i} \max(0,f(x_i;W)_j - f(x_i;W)_{y_i} + 1) \end{aligned}$ 

## E.g. Suppose that we found a W such that L = 0. Is this W unique?

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$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

#### Before:

- $= \max(0, 1.3 4.9 + 1)$ 
  - $+\max(0, 2.0 4.9 + 1)$
- $= \max(0, -2.6) + \max(0, -1.9)$

= 0 + 0

#### = 0

#### With W twice as large:

- $= \max(0, 2.6 9.8 + 1)$
- $+\max(0, 4.0 9.8 + 1)$
- $= \max(0, -6.2) + \max(0, -4.8)$
- = 0 + 0

= 0

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$$f(x,W) = Wx$$
An example:  
What is the loss? (POLL  
Cat
1.3  
car
2.5  
frog
2.0

#### Loss:

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$$f(x,W) = Wx$$
An example:  
What is the loss?
  
Cat
1.3
  
car
2.5
  
frog
2.0
  
Loss:
0.5

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$$f(x,W) = Wx$$
An example:  
What is the loss?  
How could we change W to eliminate  
the loss? (POLL)  
Cat 1.3  
car 2.5  
frog 2.0  
Loss: 0.5

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$$f(x,W)=Wx$$



An example: What is the loss?

How could we change W to eliminate the loss? (POLL)

Multiply W (and b) by 2!

cat	1.3	2.6
car	2.5	5.0
frog	2.0	4.0
Loss:	0.5	0

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$$f(x,W) = Wx$$



An example: What is the loss?

How could we change W to eliminate the loss? (POLL)

Multiply W (and b) by 2!

Wait a minute! Have we done anything useful???

cat	1.3	2.6
car	2.5	5.0
frog	2.0	4.0
Loss:	0.5	0

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$$f(x,W) = Wx$$



cat	1.3	2.6	
car	2.5	5.0	
frog	2.0	4.0	
Loss:	0.5	0	

An example: What is the loss?

How could we change W to eliminate the loss? (POLL)

Multiply W (and b) by 2!

Wait a minute! Have we done anything useful???

No! Any example that used to be wrong is still wrong (on the wrong side of the boundary). Any example that is right is still right (on the correct side of the boundary).

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### Regularization

 $\lambda$  = regularization strength (hyperparameter)

$$L(W) = \underbrace{\frac{1}{N} \sum_{i=1}^{N} L_i(f(x_i, W), y_i) + \lambda R(W)}_{(W)}$$

**Data loss**: Model predictions should match training data

**Regularization**: Prevent the model from having too much flexibility.

#### Simple examples

L2 regularization:  $R(W) = \sum_{k} \sum_{l} W_{k,l}^2$ L1 regularization:  $R(W) = \sum_{k} \sum_{l} |W_{k,l}|$ Elastic net (L1 + L2):  $R(W) = \sum_{k} \sum_{l} \beta W_{k,l}^2$  +

#### More complex:

Dropout

**Batch normalization** 

Elastic net (L1 + L2):  $R(W) = \sum_k \sum_l \beta W_{k,l}^2 + |W_{k,l}|$  Stochastic depth, fractional pooling, etc

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### Regularization

 $\lambda$  = regularization strength (hyperparameter)

$$L(W) = \frac{1}{N} \sum_{i=1}^{N} L_i(f(x_i, W), y_i) + \lambda R(W)$$

**Data loss**: Model predictions should match training data

**Regularization**: Prevent the model from having too much flexibility.

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Why regularize?

- Express preferences over weights
- Make the model simple so it works on test data
- Improve optimization by adding curvature

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### **Regularization: Expressing Preferences**

$$x = [1, 1, 1, 1]$$
  
 $w_1 = [1, 0, 0, 0]$ 

L2 Regularization
$$R(W) = \sum_k \sum_l W_{k,l}^2$$

 $w_2 = \left[0.25, 0.25, 0.25, 0.25 
ight]$ 

$$w_1^T x = w_2^T x = 1$$

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### **Regularization: Expressing Preferences**

$$x = [1, 1, 1, 1]$$
 $w_1 = [1, 0, 0, 0]$ 

L2 Regularization
$$R(W) = \sum_k \sum_l W_{k,l}^2$$

$$w_2 = \left[0.25, 0.25, 0.25, 0.25 
ight]$$

L2 regularization likes to "spread out" the weights

$$w_1^T x = w_2^T x = 1$$

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### **Regularization: Prefer Simpler Models**



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### **Regularization: Prefer Simpler Models**



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### **Regularization: Prefer Simpler Models**



Regularization pushes against fitting the data with too much flexibility. If you are going to use a complex function to fit the data, you should be doing based on a lot of data!

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### Regularization

 $\lambda$  = regularization strength (hyperparameter)

$$L(W) = \frac{1}{N} \sum_{i=1}^{N} L_i(f(x_i, W), y_i) + \lambda R(W)$$

**Data loss**: Model predictions should match training data

**Regularization**: Prevent the model from having too much flexibility.

Why not force W to have a FIXED MAGNITUDE?

For example: |W| = 1.

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### Regularization

 $\lambda$  = regularization strength (hyperparameter)

$$L(W) = \underbrace{\frac{1}{N} \sum_{i=1}^{N} L_i(f(x_i, W), y_i) + \lambda R(W)}_{\swarrow}$$

**Data loss**: Model predictions should match training data

**Regularization**: Prevent the model from having too much flexibility.

Why not force W to have a FIXED MAGNITUDE?

For example: |W| = 1.

Could be OK, but makes the optimization process more challenging. Will say more about later.

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cat**3.2**car5.1frog-1.7

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scores = unnormalized log probabilities of the classes.

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$$s=f(x_i;W)$$

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#### scores = unnormalized log probabilities of the classes.

where

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$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$

$$s=f(x_i;W)$$

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cat	3.2
car	5.1
frog	-1.7

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scores = unnormalized log probabilities of the classes.

$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$

where

$$s=f(x_i;W)$$



#### Softmax function

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3.2

5.1

-1.7

cat

car

frog

scores = unnormalized log probabilities of the classes.

$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$

where

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$$s=f(x_i;W)$$

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Want to maximize the log likelihood, or (for a loss function) to minimize the negative log likelihood of the correct class:

$$L_i = -\log P(Y=y_i|X=x_i)$$

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3.2

5.1

cat

car

frog

scores = unnormalized log probabilities of the classes.

where

$$P(Y=k|X=x_i)=rac{e^{s_k}}{\sum_j e^{s_j}}$$

$$s=f(x_i;W)$$

Want to maximize the log likelihood, or (for a loss function) to minimize the negative log likelihood of the correct class:

$$L_i = -\log P(Y=y_i|X=x_i)$$

-1.7 in summary:  $L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$ 

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cat

car

frog

$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

unnormalized log probabilities

-1.7

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$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

unnormalized probabilities



#### unnormalized log probabilities

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Softmax vs. SVM

$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

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### Softmax vs. SVM

$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$

$$L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$$

assume scores:  
[10, -2, 3]  
[10, 9, 9]  
[10, -100, -100]  
and 
$$y_i = 0$$

Q: Suppose I take a datapoint and I jiggle a bit (changing its score slightly). What happens to the loss in both cases?

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### Interactive Web Demo time....



http://vision.stanford.edu/teaching/cs231n/linear-classify-demo/

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### Recap

- We have some dataset of (x,y)
- We have a **score function**:

$$L_i = -\log(rac{e^{sy_i}}{\sum_j e^{s_j}})$$
 SVM $L_i = \sum_{j 
eq y_i} \max(0, s_j - s_{y_i} + 1)$  $L = rac{1}{N} \sum_{i=1}^N L_i + R(W)$  Full loss

$$s=f(x;W)\stackrel{ ext{e.g.}}{=}Wx$$



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# Optimization

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#### Strategy #1: A first very bad idea solution: Random search

```
# assume X train is the data where each column is an example (e.g. 3073 x 50,000)
# assume Y train are the labels (e.g. 1D array of 50,000)
# assume the function L evaluates the loss function
bestloss = float("inf") # Python assigns the highest possible float value
for num in xrange(1000):
 W = np.random.randn(10, 3073) * 0.0001 # generate random parameters
 loss = L(X train, Y train, W) # get the loss over the entire training set
 if loss < bestloss: # keep track of the best solution
   bestloss = loss
   bestW = W
 print 'in attempt %d the loss was %f, best %f' % (num, loss, bestloss)
# prints:
# in attempt 0 the loss was 9.401632, best 9.401632
# in attempt 1 the loss was 8.959668, best 8.959668
# in attempt 2 the loss was 9.044034, best 8.959668
# in attempt 3 the loss was 9.278948, best 8.959668
# in attempt 4 the loss was 8.857370, best 8.857370
# in attempt 5 the loss was 8.943151, best 8.857370
# in attempt 6 the loss was 8.605604, best 8.605604
# ... (trunctated: continues for 1000 lines)
```

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#### Let's see how well this works on the test set...

# Assume X\_test is [3073 x 10000], Y\_test [10000 x 1]
scores = Wbest.dot(Xte\_cols) # 10 x 10000, the class scores for all test examples
# find the index with max score in each column (the predicted class)
Yte\_predict = np.argmax(scores, axis = 0)
# and calculate accuracy (fraction of predictions that are correct)
np.mean(Yte\_predict == Yte)
# returns 0.1555

# 15.5% accuracy! not bad! (SOTA is ~95%)

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#### How often should I expect a random search to find a new improved solution? (POLL)

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